

# Package ‘sgs’

November 28, 2024

**Title** Sparse-Group SLOPE: Adaptive Bi-Level Selection with FDR Control

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**Description** Implementation of Sparse-group SLOPE (SGS) (Feser and Evangelou (2023) <[doi:10.48550/arXiv.2305.09467](https://doi.org/10.48550/arXiv.2305.09467)>) models. Linear and logistic regression models are supported, both of which can be fit using k-fold cross-validation. Dense and sparse input matrices are supported. In addition, a general Adaptive Three Operator Splitting (ATOS) (Pedregosa and Gidel (2018) <[doi:10.48550/arXiv.1804.02339](https://doi.org/10.48550/arXiv.1804.02339)>) implementation is provided. Group SLOPE (gSLOPE) (Brzyski et al. (2019) <[doi:10.1080/01621459.2017.1411269](https://doi.org/10.1080/01621459.2017.1411269)>) and group-based OSCAR models (Feser and Evangelou (2024) <[doi:10.48550/arXiv.2405.15357](https://doi.org/10.48550/arXiv.2405.15357)>) are also implemented. All models are available with strong screening rules (Feser and Evangelou (2024) <[doi:10.48550/arXiv.2405.15357](https://doi.org/10.48550/arXiv.2405.15357)>) for computational speed-up.

**Imports** Matrix, MASS, caret, grDevices, graphics, methods, stats, SLOPE, Rlab, Rcpp (>= 1.0.10)

**LinkingTo** Rcpp, RcppArmadillo

**Suggests** SGL, gglasso, glmnet, testthat, knitr, grpSLOPE, rmarkdown

**RoxygenNote** 7.3.1

**License** GPL (>= 3)

**Encoding** UTF-8

**URL** <https://github.com/ff1201/sgs>

**BugReports** <https://github.com/ff1201/sgs/issues>

**VignetteBuilder** knitr

**NeedsCompilation** yes

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**Repository** CRAN

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arma\_mv

*Matrix Product in RcppArmadillo.*

---

### Description

Matrix Product in RcppArmadillo.

### Usage

arma\_mv(m, v)

### Arguments

|   |                |
|---|----------------|
| m | numeric matrix |
| v | numeric vector |

### Value

matrix product of m and v

---

|             |   |
|-------------|---|
| arma_sparse | <i>Matrix Product in RcppArmadillo.</i> |
|-------------|---|

---

**Description**

Matrix Product in RcppArmadillo.

**Usage**

```
arma_sparse(m, v)
```

**Arguments**

|   |                       |
|---|-----------------------|
| m | numeric sparse matrix |
| v | numeric vector        |

**Value**

matrix product of m and v

---

|        |   |
|--------|---|
| as_sgs | <i>Fits the adaptively scaled SGS model (AS-SGS).</i> |
|--------|---|

---

**Description**

Fits an SGS model using the noise estimation procedure, termed adaptively scaled SGS (Algorithm 2 from Feser and Evangelou (2023)). This adaptively estimates  $\lambda$  and then fits the model using the estimated value. It is an alternative approach to cross-validation ([fit\\_sgs\\_cv\(\)](#)). The approach is only compatible with the SGS penalties.

**Usage**

```
as_sgs(  
  X,  
  y,  
  groups,  
  type = "linear",  
  pen_method = 2,  
  alpha = 0.95,  
  vFDR = 0.1,  
  gFDR = 0.1,  
  standardise = "l2",  
  intercept = TRUE,  
  verbose = FALSE  
)
```

**Arguments**

|                          |   |
|--------------------------|---|
| <code>X</code>           | Input matrix of dimensions $n \times p$ . Can be a sparse matrix (using class "sparseMatrix" from the Matrix package).  |
| <code>y</code>           | Output vector of dimension $n$ . For <code>type="linear"</code> should be continuous and for <code>type="logistic"</code> should be a binary variable.  |
| <code>groups</code>      | A grouping structure for the input data. Should take the form of a vector of group indices.   |
| <code>type</code>        | The type of regression to perform. Supported values are: "linear" and "logistic".   |
| <code>pen_method</code>  | The type of penalty sequences to use. <ul style="list-style-type: none"> <li>• "1" uses the vMean and gMean SGS sequences.</li> <li>• "2" uses the vMax and gMax SGS sequences.</li> </ul>  |
| <code>alpha</code>       | The value of $\alpha$ , which defines the convex balance between SLOPE and gSLOPE. Must be between 0 and 1.   |
| <code>vFDR</code>        | Defines the desired variable false discovery rate (FDR) level, which determines the shape of the variable penalties. Must be between 0 and 1.   |
| <code>gFDR</code>        | Defines the desired group false discovery rate (FDR) level, which determines the shape of the group penalties. Must be between 0 and 1.   |
| <code>standardise</code> | Type of standardisation to perform on $X$ : <ul style="list-style-type: none"> <li>• "l2" standardises the input data to have <math>\ell_2</math> norms of one.</li> <li>• "l1" standardises the input data to have <math>\ell_1</math> norms of one.</li> <li>• "sd" standardises the input data to have standard deviation of one.</li> <li>• "none" no standardisation applied.</li> </ul> |
| <code>intercept</code>   | Logical flag for whether to fit an intercept.   |
| <code>verbose</code>     | Logical flag for whether to print fitting information.  |

**Value**

An object of type "sgs" containing model fit information (see `fit_sgs()`).

**References**

Feser, F., Evangelou, M. (2023). *Sparse-group SLOPE: adaptive bi-level selection with FDR-control*, <https://arxiv.org/abs/2305.09467>

**See Also**

`scaled_sgs()`

Other model-selection: `fit_goscar_cv()`, `fit_gslope_cv()`, `fit_sgo_cv()`, `fit_sgs_cv()`, `scaled_sgs()`

Other SGS-methods: `coef.sgs()`, `fit_sgo()`, `fit_sgo_cv()`, `fit_sgs()`, `fit_sgs_cv()`, `plot.sgs()`, `predict.sgs()`, `print.sgs()`, `scaled_sgs()`

---

 atos

*Adaptive three operator splitting (ATOS).*


---

### Description

Function for fitting adaptive three operator splitting (ATOS) with general convex penalties. Supports both linear and logistic regression, both with dense and sparse matrix implementations.

### Usage

```
atos(
  X,
  y,
  type = "linear",
  prox_1,
  prox_2,
  pen_prox_1 = 0.5,
  pen_prox_2 = 0.5,
  max_iter = 5000,
  backtracking = 0.7,
  max_iter_backtracking = 100,
  tol = 1e-05,
  prox_1_opts = NULL,
  prox_2_opts = NULL,
  standardise = "l2",
  intercept = TRUE,
  x0 = NULL,
  u = NULL,
  verbose = FALSE
)
```

### Arguments

|              |   |
|--------------|---|
| X            | Input matrix of dimensions $n \times p$ . Can be a sparse matrix (using class "sparseMatrix" from the Matrix package)   |
| y            | Output vector of dimension $n$ . For type="linear" needs to be continuous and for type="logistic" needs to be a binary variable.                                |
| type         | The type of regression to perform. Supported values are: "linear" and "logistic".   |
| prox_1       | The proximal operator for the first function, $h(x)$ .  |
| prox_2       | The proximal operator for the second function, $g(x)$ .   |
| pen_prox_1   | The penalty for the first proximal operator. For the lasso, this would be the sparsity parameter, $\lambda$ . If operator does not include a penalty, set to 1. |
| pen_prox_2   | The penalty for the second proximal operator.   |
| max_iter     | Maximum number of ATOS iterations to perform.   |
| backtracking | The backtracking parameter, $\tau$ , as defined in Pedregosa and Gidel (2018).  |

|                       |   |
|-----------------------|---|
| max_iter_backtracking | Maximum number of backtracking line search iterations to perform per global iteration.  |
| tol                   | Convergence tolerance for the stopping criteria.  |
| prox_1_opts           | Optional argument for first proximal operator. For the group lasso, this would be the group IDs. Note: this must be inserted as a list.   |
| prox_2_opts           | Optional argument for second proximal operator.   |
| standardise           | Type of standardisation to perform on $X$ : <ul style="list-style-type: none"> <li>• "l2" standardises the input data to have <math>\ell_2</math> norms of one.</li> <li>• "l1" standardises the input data to have <math>\ell_1</math> norms of one.</li> <li>• "sd" standardises the input data to have standard deviation of one.</li> <li>• "none" no standardisation applied.</li> </ul> |
| intercept             | Logical flag for whether to fit an intercept.   |
| x0                    | Optional initial vector for $x_0$ .   |
| u                     | Optional initial vector for $u$ .   |
| verbose               | Logical flag for whether to print fitting information.  |

### Details

atos() solves convex minimization problems of the form

$$f(x) + g(x) + h(x),$$

where  $f$  is convex and differentiable with  $L_f$ -Lipschitz gradient, and  $g$  and  $h$  are both convex. The algorithm is not symmetrical, but usually the difference between variations are only small numerical values, which are filtered out. However, both variations should be checked regardless, by looking at  $x$  and  $u$ . An example for the sparse-group lasso (SGL) is given.

### Value

An object of class "atos" containing:

|             |   |
|-------------|---|
| beta        | The fitted values from the regression. Taken to be the more stable fit between $x$ and $u$ , which is usually the former. |
| x           | The solution to the original problem (see Pedregosa and Gidel (2018)).  |
| u           | The solution to the dual problem (see Pedregosa and Gidel (2018)).  |
| z           | The updated values from applying the first proximal operator (see Pedregosa and Gidel (2018)).                            |
| type        | Indicates which type of regression was performed.   |
| success     | Logical flag indicating whether ATOS converged, according to tol.   |
| num_it      | Number of iterations performed. If convergence is not reached, this will be max_iter.                                     |
| certificate | Final value of convergence criteria.  |
| intercept   | Logical flag indicating whether an intercept was fit.   |

## References

Pedregosa, F., Gidel, G. (2018). *Adaptive Three Operator Splitting*, <https://proceedings.mlr.press/v80/pedregosa18a.html>

---

|          |   |
|----------|---|
| coef.sgs | <i>Extracts coefficients for one of the following object types: "sgs", "sgs_cv", "gslope", "gslope_cv".</i> |
|----------|---|

---

## Description

Print the coefficients using model fitted with one of the following functions: `fit_sgs()`, `fit_sgs_cv()`, `fit_gslope()`, `fit_gslope_cv()`, `fit_sgo()`, `fit_sgo_cv()`, `fit_goscar()`, `fit_goscar_cv()`. The predictions are calculated for each "lambda" value in the path.

## Usage

```
## S3 method for class 'sgs'
coef(object, ...)
```

## Arguments

|        |   |
|--------|---|
| object | Object of one of the following classes: "sgs", "sgs_cv", "gslope", "gslope_cv". |
| ...    | further arguments passed to stats function.                                     |

## Value

The fitted coefficients

## See Also

`fit_sgs()`, `fit_sgs_cv()`, `fit_gslope()`, `fit_gslope_cv()`

Other SGS-methods: `as_sgs()`, `fit_sgo()`, `fit_sgo_cv()`, `fit_sgs()`, `fit_sgs_cv()`, `plot.sgs()`, `predict.sgs()`, `print.sgs()`, `scaled_sgs()`

Other gSLOPE-methods: `fit_goscar()`, `fit_goscar_cv()`, `fit_gslope()`, `fit_gslope_cv()`, `plot.sgs()`, `predict.sgs()`, `print.sgs()`

## Examples

```
# specify a grouping structure
groups = c(1,1,1,2,2,3,3,3,4,4)
# generate data
data = gen_toy_data(p=10, n=5, groups = groups, seed_id=3,group_sparsity=1)
# run SGS
model = fit_sgs(X = data$X, y = data$y, groups = groups, type="linear", lambda = 1, alpha=0.95,
vFDR=0.1, gFDR=0.1, standardise = "l2", intercept = TRUE, verbose=FALSE)
# use predict function
model_coef = coef(model)
```

---

 fit\_goscar

*Fit a gOSCAR model.*


---

### Description

Group OSCAR (gOSCAR) main fitting function. Supports both linear and logistic regression, both with dense and sparse matrix implementations.

### Usage

```
fit_goscar(
  X,
  y,
  groups,
  type = "linear",
  lambda = "path",
  path_length = 20,
  min_frac = 0.05,
  max_iter = 5000,
  backtracking = 0.7,
  max_iter_backtracking = 100,
  tol = 1e-05,
  standardise = "l2",
  intercept = TRUE,
  screen = TRUE,
  verbose = FALSE,
  w_weights = NULL
)
```

### Arguments

|        |   |
|--------|---|
| X      | Input matrix of dimensions $n \times p$ . Can be a sparse matrix (using class "sparseMatrix" from the Matrix package).  |
| y      | Output vector of dimension $n$ . For type="linear" should be continuous and for type="logistic" should be a binary variable.  |
| groups | A grouping structure for the input data. Should take the form of a vector of group indices.   |
| type   | The type of regression to perform. Supported values are: "linear" and "logistic".   |
| lambda | The regularisation parameter. Defines the level of sparsity in the model. A higher value leads to sparser models: <ul style="list-style-type: none"> <li>"path" computes a path of regularisation parameters of length "path_length". The path will begin just above the value at which the first predictor enters the model and will terminate at the value determined by min_frac.</li> <li>User-specified single value or sequence. Internal scaling is applied based on the type of standardisation. The returned "lambda" value will be the original unscaled value(s).</li> </ul> |



|                       |  |
|-----------------------|--|
| path_length           | The number of $\lambda$ values to fit the model for. If "lambda" is user-specified, this is ignored.   |
| min_frac              | Smallest value of $\lambda$ as a fraction of the maximum value. That is, the final $\lambda$ will be "min_frac" of the first $\lambda$ value.  |
| max_iter              | Maximum number of ATOS iterations to perform.  |
| backtracking          | The backtracking parameter, $\tau$ , as defined in Pedregosa and Gidel (2018).   |
| max_iter_backtracking | Maximum number of backtracking line search iterations to perform per global iteration.   |
| tol                   | Convergence tolerance for the stopping criteria.   |
| standardise           | Type of standardisation to perform on $X$ : <ul style="list-style-type: none"> <li>• "l2" standardises the input data to have <math>\ell_2</math> norms of one. When using this "lambda" is scaled internally by <math>1/\sqrt{n}</math>.</li> <li>• "l1" standardises the input data to have <math>\ell_1</math> norms of one. When using this "lambda" is scaled internally by <math>1/n</math>.</li> <li>• "sd" standardises the input data to have standard deviation of one.</li> <li>• "none" no standardisation applied.</li> </ul> |
| intercept             | Logical flag for whether to fit an intercept.  |
| screen                | Logical flag for whether to apply screening rules (see Feser and Evangelou (2024)). Screening discards irrelevant groups before fitting, greatly improving speed.  |
| verbose               | Logical flag for whether to print fitting information.   |
| w_weights             | Optional vector for the group penalty weights. Overrides the OSCAR penalties when specified. When entering custom weights, these are multiplied internally by $\lambda$ . To void this behaviour, set $\lambda = 1$ .  |

## Details

`fit_goscar()` fits a gOSCAR model (Feser and Evangelou (2024)) using adaptive three operator splitting (ATOS). gOSCAR uses the same model set-up as for gSLOPE, but with different weights (see Bao et al. (2020) and Feser and Evangelou (2024)). The penalties are given by (for a group  $g$  with  $m$  groups):

$$w_g = \sigma_1 + \sigma_3(m - g),$$

where

$$\sigma_1 = d_i \|X^T y\|_\infty, \quad \sigma_3 = \sigma_1/m.$$

## Value

A list containing:

|      |   |
|------|---|
| beta | The fitted values from the regression. Taken to be the more stable fit between $x$ and $z$ , which is usually the former. A filter is applied to remove very small values, where ATOS has not been able to shrink exactly to zero. Check this against $x$ and $z$ . |
|------|---|

|                |   |
|----------------|---|
| group_effects  | The group values from the regression. Taken by applying the $\ell_2$ norm within each group on beta.  |
| selected_var   | A list containing the indices of the active/selected variables for each "lambda" value. Index 1 corresponds to the first column in X.             |
| selected_grp   | A list containing the indices of the active/selected groups for each "lambda" value. Index 1 corresponds to the first group in the groups vector. |
| num_it         | Number of iterations performed. If convergence is not reached, this will be max_iter.   |
| success        | Logical flag indicating whether ATOS converged, according to tol.   |
| certificate    | Final value of convergence criteria.  |
| x              | The solution to the original problem (see Pedregosa and Gidel (2018)).  |
| u              | The solution to the dual problem (see Pedregosa and Gidel (2018)).  |
| z              | The updated values from applying the first proximal operator (see Pedregosa and Gidel (2018)).  |
| screen_set     | List of groups that were kept after screening step for each "lambda" value. (corresponds to $\mathcal{S}$ in Feser and Evangelou (2024)).         |
| epsilon_set    | List of groups that were used for fitting after screening for each "lambda" value. (corresponds to $\mathcal{E}$ in Feser and Evangelou (2024)).  |
| kkt_violations | List of groups that violated the KKT conditions each "lambda" value. (corresponds to $\mathcal{K}$ in Feser and Evangelou (2024)).                |
| pen_gslope     | Vector of the group penalty sequence.   |
| screen         | Logical flag indicating whether screening was applied.  |
| type           | Indicates which type of regression was performed.   |
| intercept      | Logical flag indicating whether an intercept was fit.   |
| standardise    | Type of standardisation used.   |
| lambda         | Value(s) of $\lambda$ used to fit the model.  |

## References

- Bao, R., Gu B., Huang, H. (2020). *Fast OSCAR and OWL Regression via Safe Screening Rules*, <https://proceedings.mlr.press/v119/bao20b>
- Feser, F., Evangelou, M. (2024). *Strong screening rules for group-based SLOPE models*, <https://proceedings.mlr.press/v80/pedregosa18a.html>
- Pedregosa, F., Gidel, G. (2018). *Adaptive Three Operator Splitting*, <https://proceedings.mlr.press/v80/pedregosa18a.html>

## See Also

Other gSLOPE-methods: [coef.sgs\(\)](#), [fit\\_goscar\\_cv\(\)](#), [fit\\_gslope\(\)](#), [fit\\_gslope\\_cv\(\)](#), [plot.sgs\(\)](#), [predict.sgs\(\)](#), [print.sgs\(\)](#)

**Examples**

```
# specify a grouping structure
groups = c(1,1,1,2,2,3,3,3,4,4)
# generate data
data = gen_toy_data(p=10, n=5, groups = groups, seed_id=3,group_sparsity=1)
# run gOSCAR
model = fit_goscar(X = data$X, y = data$y, groups = groups, type="linear", path_length = 5,
standardise = "l2", intercept = TRUE, verbose=FALSE)
```

---

fit\_goscar\_cv

*Fit a gOSCAR model using k-fold cross-validation.*


---

**Description**

Function to fit a pathwise solution of group OSCAR (gOSCAR) models using k-fold cross-validation. Supports both linear and logistic regression, both with dense and sparse matrix implementations.

**Usage**

```
fit_goscar_cv(
  X,
  y,
  groups,
  type = "linear",
  lambda = "path",
  path_length = 20,
  min_frac = 0.05,
  nfolds = 10,
  backtracking = 0.7,
  max_iter = 5000,
  max_iter_backtracking = 100,
  tol = 1e-05,
  standardise = "l2",
  intercept = TRUE,
  error_criteria = "mse",
  screen = TRUE,
  verbose = FALSE,
  w_weights = NULL
)
```

**Arguments**

|   |  |
|---|--|
| X | Input matrix of dimensions $n \times p$ . Can be a sparse matrix (using class "sparseMatrix" from the Matrix package).       |
| y | Output vector of dimension $n$ . For type="linear" should be continuous and for type="logistic" should be a binary variable. |

|                       |   |
|-----------------------|---|
| groups                | A grouping structure for the input data. Should take the form of a vector of group indices.   |
| type                  | The type of regression to perform. Supported values are: "linear" and "logistic".   |
| lambda                | The regularisation parameter. Defines the level of sparsity in the model. A higher value leads to sparser models: <ul style="list-style-type: none"> <li>• "path" computes a path of regularisation parameters of length "path_length". The path will begin just above the value at which the first predictor enters the model and will terminate at the value determined by "min_frac".</li> <li>• User-specified single value or sequence. Internal scaling is applied based on the type of standardisation. The returned "lambda" value will be the original unscaled value(s).</li> </ul> |
| path_length           | The number of $\lambda$ values to fit the model for. If "lambda" is user-specified, this is ignored.  |
| min_frac              | Smallest value of $\lambda$ as a fraction of the maximum value. That is, the final $\lambda$ will be "min_frac" of the first $\lambda$ value.   |
| nfolds                | The number of folds to use in cross-validation.   |
| backtracking          | The backtracking parameter, $\tau$ , as defined in Pedregosa and Gidel (2018).  |
| max_iter              | Maximum number of ATOS iterations to perform.   |
| max_iter_backtracking | Maximum number of backtracking line search iterations to perform per global iteration.  |
| tol                   | Convergence tolerance for the stopping criteria.  |
| standardise           | Type of standardisation to perform on $X$ : <ul style="list-style-type: none"> <li>• "l2" standardises the input data to have <math>\ell_2</math> norms of one.</li> <li>• "l1" standardises the input data to have <math>\ell_1</math> norms of one.</li> <li>• "sd" standardises the input data to have standard deviation of one.</li> <li>• "none" no standardisation applied.</li> </ul>   |
| intercept             | Logical flag for whether to fit an intercept.   |
| error_criteria        | The criteria used to discriminate between models along the path. Supported values are: "mse" (mean squared error) and "mae" (mean absolute error).  |
| screen                | Logical flag for whether to apply screening rules (see Feser and Evangelou (2024)). Screening discards irrelevant groups before fitting, greatly improving speed.   |
| verbose               | Logical flag for whether to print fitting information.  |
| w_weights             | Optional vector for the group penalty weights. Overrides the OSCAR penalties when specified. When entering custom weights, these are multiplied internally by $\lambda$ . To void this behaviour, set $\lambda = 1$ .   |

### Details

Fits gOSCAR models under a pathwise solution using adaptive three operator splitting (ATOS), picking the 1se model as optimum. Warm starts are implemented.

**Value**

A list containing:

|                |  |
|----------------|--|
| errors         | A table containing fitting information about the models on the path.                 |
| all_models     | Fitting information for all models fit on the path, which is a "gslope" object type. |
| fit            | The 1st chosen model, which is a "gslope" object type.                               |
| best_lambda    | The value of $\lambda$ which generated the chosen model.                             |
| best_lambda_id | The path index for the chosen model.   |

**References**

Bao, R., Gu B., Huang, H. (2020). *Fast OSCAR and OWL Regression via Safe Screening Rules*, <https://proceedings.mlr.press/v119/bao20b>

Feser, F., Evangelou, M. (2024). *Strong screening rules for group-based SLOPE models*, <https://proceedings.mlr.press/v80/pedregosa18a.html>

**See Also**

[fit\\_goscar\(\)](#)

Other gSLOPE-methods: [coef.sgs\(\)](#), [fit\\_goscar\(\)](#), [fit\\_gslope\(\)](#), [fit\\_gslope\\_cv\(\)](#), [plot.sgs\(\)](#), [predict.sgs\(\)](#), [print.sgs\(\)](#)

Other model-selection: [as\\_sgs\(\)](#), [fit\\_gslope\\_cv\(\)](#), [fit\\_sgo\\_cv\(\)](#), [fit\\_sgs\\_cv\(\)](#), [scaled\\_sgs\(\)](#)

**Examples**

```
# specify a grouping structure
groups = c(1,1,1,2,2,3,3,3,4,4)
# generate data
data = gen_toy_data(p=10, n=5, groups = groups, seed_id=3,group_sparsity=1)
# run gOSCAR with cross-validation
cv_model = fit_goscar_cv(X = data$X, y = data$y, groups=groups, type = "linear", path_length = 5,
nolds=5, min_frac = 0.05, standardise="l2",intercept=TRUE,verbose=TRUE)
```

---

fit\_gslope

*Fit a gSLOPE model.*

---

**Description**

Group SLOPE (gSLOPE) main fitting function. Supports both linear and logistic regression, both with dense and sparse matrix implementations.

**Usage**

```
fit_gslope(
  X,
  y,
  groups,
  type = "linear",
  lambda = "path",
  path_length = 20,
  min_frac = 0.05,
  gFDR = 0.1,
  pen_method = 1,
  max_iter = 5000,
  backtracking = 0.7,
  max_iter_backtracking = 100,
  tol = 1e-05,
  standardise = "l2",
  intercept = TRUE,
  screen = TRUE,
  verbose = FALSE,
  w_weights = NULL
)
```

**Arguments**

|             |   |
|-------------|---|
| X           | Input matrix of dimensions $n \times p$ . Can be a sparse matrix (using class "sparseMatrix" from the Matrix package).  |
| y           | Output vector of dimension $n$ . For type="linear" should be continuous and for type="logistic" should be a binary variable.  |
| groups      | A grouping structure for the input data. Should take the form of a vector of group indices.   |
| type        | The type of regression to perform. Supported values are: "linear" and "logistic".   |
| lambda      | The regularisation parameter. Defines the level of sparsity in the model. A higher value leads to sparser models: <ul style="list-style-type: none"> <li>"path" computes a path of regularisation parameters of length "path_length". The path will begin just above the value at which the first predictor enters the model and will terminate at the value determined by "min_frac".</li> <li>User-specified single value or sequence. Internal scaling is applied based on the type of standardisation. The returned "lambda" value will be the original unscaled value(s).</li> </ul> |
| path_length | The number of $\lambda$ values to fit the model for. If "lambda" is user-specified, this is ignored.  |
| min_frac    | Smallest value of $\lambda$ as a fraction of the maximum value. That is, the final $\lambda$ will be "min_frac" of the first $\lambda$ value.   |
| gFDR        | Defines the desired group false discovery rate (FDR) level, which determines the shape of the group penalties. Must be between 0 and 1.   |

|                       |  |
|-----------------------|--|
| pen_method            | The type of penalty sequences to use (see Brzyski et al. (2019)): <ul style="list-style-type: none"> <li>• "1" uses the gMean gSLOPE sequence.</li> <li>• "2" uses the gMax gSLOPE sequence.</li> </ul>  |
| max_iter              | Maximum number of ATOS iterations to perform.  |
| backtracking          | The backtracking parameter, $\tau$ , as defined in Pedregosa and Gidel (2018).   |
| max_iter_backtracking | Maximum number of backtracking line search iterations to perform per global iteration.   |
| tol                   | Convergence tolerance for the stopping criteria.   |
| standardise           | Type of standardisation to perform on $X$ : <ul style="list-style-type: none"> <li>• "l2" standardises the input data to have <math>\ell_2</math> norms of one. When using this "lambda" is scaled internally by <math>1/\sqrt{n}</math>.</li> <li>• "l1" standardises the input data to have <math>\ell_1</math> norms of one. When using this "lambda" is scaled internally by <math>1/n</math>.</li> <li>• "sd" standardises the input data to have standard deviation of one.</li> <li>• "none" no standardisation applied.</li> </ul> |
| intercept             | Logical flag for whether to fit an intercept.  |
| screen                | Logical flag for whether to apply screening rules (see Feser and Evangelou (2024)). Screening discards irrelevant groups before fitting, greatly improving speed.  |
| verbose               | Logical flag for whether to print fitting information.   |
| w_weights             | Optional vector for the group penalty weights. Overrides the penalties from pen_method if specified. When entering custom weights, these are multiplied internally by $\lambda$ . To void this behaviour, set $\lambda = 1$ .  |

## Details

`fit_gslope()` fits a gSLOPE model (Brzyski et al. (2019)) using adaptive three operator splitting (ATOS). gSLOPE is a sparse-group method, so that it selects both variables and groups. Unlike group selection approaches, not every variable within a group is set as active. It solves the convex optimisation problem given by

$$\frac{1}{2n} f(b; y, \mathbf{X}) + \lambda \sum_{g=1}^m w_g \sqrt{p_g} \|b^{(g)}\|_2,$$

where the penalty sequences are sorted and  $f(\cdot)$  is the loss function. In the case of the linear model, the loss function is given by the mean-squared error loss:

$$f(b; y, \mathbf{X}) = \|y - \mathbf{X}b\|_2^2.$$

In the logistic model, the loss function is given by

$$f(b; y, \mathbf{X}) = -1/n \log(\mathcal{L}(b; y, \mathbf{X})).$$

where the log-likelihood is given by

$$\mathcal{L}(b; y, \mathbf{X}) = \sum_{i=1}^n \{y_i b^\top x_i - \log(1 + \exp(b^\top x_i))\}.$$

The penalty parameters in gSLOPE are sorted so that the largest group effects are matched with the largest penalties, to reduce the group FDR. The gMean sequence (pen\_method=1) is given by

$$w_i^{\text{mean}} = \bar{F}_{\chi_{p_j}}^{-1}(1 - q_g i/m), \quad i = 1, \dots, m, \quad \text{where } \bar{F}_{\chi_{p_j}}(x) := \frac{1}{m} \sum_{j=1}^m F_{\chi_{p_j}}(\sqrt{p_j}x),$$

where  $F_{\chi_{p_j}}$  is the cumulative distribution function of a  $\chi$  distribution with  $p_j$  degrees of freedom. The gMax sequence (pen\_method=2) is given by

$$w_i^{\text{max}} = \max_{j=1, \dots, m} \left\{ \frac{1}{\sqrt{p_j}} F_{\chi_{p_j}}^{-1} \left( 1 - \frac{q_g i}{m} \right) \right\},$$

where  $F_{\chi_{p_j}}$  is the cumulative distribution function of a  $\chi$  distribution with  $p_j$  degrees of freedom.

## Value

A list containing:

|                |   |
|----------------|---|
| beta           | The fitted values from the regression. Taken to be the more stable fit between x and z, which is usually the former. A filter is applied to remove very small values, where ATOS has not been able to shrink exactly to zero. Check this against x and z. |
| group_effects  | The group values from the regression. Taken by applying the $\ell_2$ norm within each group on beta.  |
| selected_var   | A list containing the indicies of the active/selected variables for each "lambda" value. Index 1 corresponds to the first column in X.  |
| selected_grp   | A list containing the indicies of the active/selected groups for each "lambda" value. Index 1 corresponds to the first group in the groups vector.  |
| num_it         | Number of iterations performed. If convergence is not reached, this will be max_iter.   |
| success        | Logical flag indicating whether ATOS converged, according to tol.   |
| certificate    | Final value of convergence criteria.  |
| x              | The solution to the original problem (see Pedregosa and Gidel (2018)).  |
| u              | The solution to the dual problem (see Pedregosa and Gidel (2018)).  |
| z              | The updated values from applying the first proximal operator (see Pedregosa and Gidel (2018)).  |
| screen_set     | List of groups that were kept after screening step for each "lambda" value. (corresponds to $\mathcal{S}$ in Feser and Evangelou (2024)).   |
| epsilon_set    | List of groups that were used for fitting after screening for each "lambda" value. (corresponds to $\mathcal{E}$ in Feser and Evangelou (2024)).  |
| kkt_violations | List of groups that violated the KKT conditions each "lambda" value. (corresponds to $\mathcal{K}$ in Feser and Evangelou (2024)).  |
| pen_gslope     | Vector of the group penalty sequence.   |
| screen         | Logical flag indicating whether screening was applied.  |
| type           | Indicates which type of regression was performed.   |
| intercept      | Logical flag indicating whether an intercept was fit.   |
| standardise    | Type of standardisation used.   |
| lambda         | Value(s) of $\lambda$ used to fit the model.  |



## References

- Brzyski, D., Gossmann, A., Su, W., Bodgan, M. (2019). *Group SLOPE – Adaptive Selection of Groups of Predictors*, <https://www.tandfonline.com/doi/full/10.1080/01621459.2017.1411269>
- Feser, F., Evangelou, M. (2024). *Strong screening rules for group-based SLOPE models*, <https://proceedings.mlr.press/v80/pedregosa18a.html>
- Pedregosa, F., Gidel, G. (2018). *Adaptive Three Operator Splitting*, <https://proceedings.mlr.press/v80/pedregosa18a.html>

## See Also

Other gSLOPE-methods: `coef.sgs()`, `fit_goscar()`, `fit_goscar_cv()`, `fit_gslope_cv()`, `plot.sgs()`, `predict.sgs()`, `print.sgs()`

## Examples

```
# specify a grouping structure
groups = c(1,1,1,2,2,3,3,3,4,4)
# generate data
data = gen_toy_data(p=10, n=5, groups = groups, seed_id=3,group_sparsity=1)
# run gSLOPE
model = fit_gslope(X = data$X, y = data$y, groups = groups, type="linear", path_length = 5,
gFDR=0.1, standardise = "l2", intercept = TRUE, verbose=FALSE)
```

---

```
fit_gslope_cv
```

```
Fit a gSLOPE model using k-fold cross-validation.
```

---

## Description

Function to fit a pathwise solution of group SLOPE (gSLOPE) models using k-fold cross-validation. Supports both linear and logistic regression, both with dense and sparse matrix implementations.

## Usage

```
fit_gslope_cv(
  X,
  y,
  groups,
  type = "linear",
  lambda = "path",
  path_length = 20,
  min_frac = 0.05,
  nfolds = 10,
  gFDR = 0.1,
  pen_method = 1,
  backtracking = 0.7,
  max_iter = 5000,
```

```

max_iter_backtracking = 100,
tol = 1e-05,
standardise = "l2",
intercept = TRUE,
error_criteria = "mse",
screen = TRUE,
verbose = FALSE,
w_weights = NULL
)

```

### Arguments

|                       |   |
|-----------------------|---|
| X                     | Input matrix of dimensions $n \times p$ . Can be a sparse matrix (using class "sparseMatrix" from the Matrix package).  |
| y                     | Output vector of dimension $n$ . For type="linear" should be continuous and for type="logistic" should be a binary variable.  |
| groups                | A grouping structure for the input data. Should take the form of a vector of group indices.   |
| type                  | The type of regression to perform. Supported values are: "linear" and "logistic".   |
| lambda                | The regularisation parameter. Defines the level of sparsity in the model. A higher value leads to sparser models: <ul style="list-style-type: none"> <li>"path" computes a path of regularisation parameters of length "path_length". The path will begin just above the value at which the first predictor enters the model and will terminate at the value determined by "min_frac".</li> <li>User-specified single value or sequence. Internal scaling is applied based on the type of standardisation. The returned "lambda" value will be the original unscaled value(s).</li> </ul> |
| path_length           | The number of $\lambda$ values to fit the model for. If "lambda" is user-specified, this is ignored.  |
| min_frac              | Smallest value of $\lambda$ as a fraction of the maximum value. That is, the final $\lambda$ will be "min_frac" of the first $\lambda$ value.   |
| nfolds                | The number of folds to use in cross-validation.   |
| gFDR                  | Defines the desired group false discovery rate (FDR) level, which determines the shape of the penalties. Must be between 0 and 1.   |
| pen_method            | The type of penalty sequences to use (see Brzyski et al. (2019)): <ul style="list-style-type: none"> <li>"1" uses the gMean gSLOPE sequence.</li> <li>"2" uses the gMax gSLOPE sequence.</li> </ul>   |
| backtracking          | The backtracking parameter, $\tau$ , as defined in Pedregosa and Gidel (2018).  |
| max_iter              | Maximum number of ATOS iterations to perform.   |
| max_iter_backtracking | Maximum number of backtracking line search iterations to perform per global iteration.  |
| tol                   | Convergence tolerance for the stopping criteria.  |
| standardise           | Type of standardisation to perform on X:  |

|                |   |
|----------------|---|
|                | <ul style="list-style-type: none"> <li>• "l2" standardises the input data to have <math>\ell_2</math> norms of one.</li> <li>• "l1" standardises the input data to have <math>\ell_1</math> norms of one.</li> <li>• "sd" standardises the input data to have standard deviation of one.</li> <li>• "none" no standardisation applied.</li> </ul> |
| intercept      | Logical flag for whether to fit an intercept.   |
| error_criteria | The criteria used to discriminate between models along the path. Supported values are: "mse" (mean squared error) and "mae" (mean absolute error).  |
| screen         | Logical flag for whether to apply screening rules (see Feser and Evangelou (2024)). Screening discards irrelevant groups before fitting, greatly improving speed.   |
| verbose        | Logical flag for whether to print fitting information.  |
| w_weights      | Optional vector for the group penalty weights. Overrides the penalties from pen_method if specified. When entering custom weights, these are multiplied internally by $\lambda$ . To void this behaviour, set $\lambda = 1$ .   |

### Details

Fits gSLOPE models under a pathwise solution using adaptive three operator splitting (ATOS), picking the 1se model as optimum. Warm starts are implemented.

### Value

A list containing:

|                |  |
|----------------|--|
| errors         | A table containing fitting information about the models on the path.                 |
| all_models     | Fitting information for all models fit on the path, which is a "gslope" object type. |
| fit            | The 1se chosen model, which is a "gslope" object type.                               |
| best_lambda    | The value of $\lambda$ which generated the chosen model.                             |
| best_lambda_id | The path index for the chosen model.   |

### References

- Brzyski, D., Gossmann, A., Su, W., Bodgan, M. (2019). *Group SLOPE – Adaptive Selection of Groups of Predictors*, <https://www.tandfonline.com/doi/full/10.1080/01621459.2017.1411269>
- Feser, F., Evangelou, M. (2024). *Strong screening rules for group-based SLOPE models*, <https://proceedings.mlr.press/v80/pedregosa18a.html>

### See Also

[fit\\_gslope\(\)](#)

Other gSLOPE-methods: [coef.sgs\(\)](#), [fit\\_goscar\(\)](#), [fit\\_goscar\\_cv\(\)](#), [fit\\_gslope\(\)](#), [plot.sgs\(\)](#), [predict.sgs\(\)](#), [print.sgs\(\)](#)

Other model-selection: [as\\_sgs\(\)](#), [fit\\_goscar\\_cv\(\)](#), [fit\\_sgo\\_cv\(\)](#), [fit\\_sgs\\_cv\(\)](#), [scaled\\_sgs\(\)](#)

**Examples**

```
# specify a grouping structure
groups = c(1,1,1,2,2,3,3,3,4,4)
# generate data
data = gen_toy_data(p=10, n=5, groups = groups, seed_id=3,group_sparsity=1)
# run gSLOPE with cross-validation
cv_model = fit_gslope_cv(X = data$X, y = data$y, groups=groups, type = "linear", path_length = 5,
nolds=5, gFDR = 0.1, min_frac = 0.05, standardise="l2",intercept=TRUE,verbose=TRUE)
```

---

fit\_sgo

*Fit an SGO model.*


---

**Description**

Sparse-group OSCAR (SGO) main fitting function. Supports both linear and logistic regression, both with dense and sparse matrix implementations.

**Usage**

```
fit_sgo(
  X,
  y,
  groups,
  type = "linear",
  lambda = "path",
  path_length = 20,
  min_frac = 0.05,
  alpha = 0.95,
  max_iter = 5000,
  backtracking = 0.7,
  max_iter_backtracking = 100,
  tol = 1e-05,
  standardise = "l2",
  intercept = TRUE,
  screen = TRUE,
  verbose = FALSE,
  w_weights = NULL,
  v_weights = NULL
)
```

**Arguments**

- |   |  |
|---|--|
| X | Input matrix of dimensions $n \times p$ . Can be a sparse matrix (using class "sparseMatrix" from the Matrix package).       |
| y | Output vector of dimension $n$ . For type="linear" should be continuous and for type="logistic" should be a binary variable. |

|                       |   |
|-----------------------|---|
| groups                | A grouping structure for the input data. Should take the form of a vector of group indices.   |
| type                  | The type of regression to perform. Supported values are: "linear" and "logistic".   |
| lambda                | The regularisation parameter. Defines the level of sparsity in the model. A higher value leads to sparser models: <ul style="list-style-type: none"> <li>• "path" computes a path of regularisation parameters of length "path_length". The path will begin just above the value at which the first predictor enters the model and will terminate at the value determined by "min_frac".</li> <li>• User-specified single value or sequence. Internal scaling is applied based on the type of standardisation. The returned "lambda" value will be the original unscaled value(s).</li> </ul> |
| path_length           | The number of $\lambda$ values to fit the model for. If "lambda" is user-specified, this is ignored.  |
| min_frac              | Smallest value of $\lambda$ as a fraction of the maximum value. That is, the final $\lambda$ will be "min_frac" of the first $\lambda$ value.   |
| alpha                 | The value of $\alpha$ , which defines the convex balance between OSCAR and gOSCAR. Must be between 0 and 1. Recommended value is 0.95.  |
| max_iter              | Maximum number of ATOS iterations to perform.   |
| backtracking          | The backtracking parameter, $\tau$ , as defined in Pedregosa and Gidel (2018).  |
| max_iter_backtracking | Maximum number of backtracking line search iterations to perform per global iteration.  |
| tol                   | Convergence tolerance for the stopping criteria.  |
| standardise           | Type of standardisation to perform on $X$ : <ul style="list-style-type: none"> <li>• "l2" standardises the input data to have <math>\ell_2</math> norms of one. When using this "lambda" is scaled internally by <math>1/\sqrt{n}</math>.</li> <li>• "l1" standardises the input data to have <math>\ell_1</math> norms of one. When using this "lambda" is scaled internally by <math>1/n</math>.</li> <li>• "sd" standardises the input data to have standard deviation of one.</li> <li>• "noBaone" no standardisation applied.</li> </ul>   |
| intercept             | Logical flag for whether to fit an intercept.   |
| screen                | Logical flag for whether to apply screening rules (see Feser and Evangelou (2024)). Screening discards irrelevant groups before fitting, greatly improving speed.   |
| verbose               | Logical flag for whether to print fitting information.  |
| w_weights             | Optional vector for the group penalty weights. Overrides the OSCAR penalties when specified. When entering custom weights, these are multiplied internally by $\lambda$ and $1 - \alpha$ . To void this behaviour, set $\lambda = 2$ and $\alpha = 0.5$ .   |
| v_weights             | Optional vector for the variable penalty weights. Overrides the OSCAR penalties when specified. When entering custom weights, these are multiplied internally by $\lambda$ and $\alpha$ . To void this behaviour, set $\lambda = 2$ and $\alpha = 0.5$ .  |

## Details

`fit_sgo()` fits an SGO model (Feser and Evangelou (2024)) using adaptive three operator splitting (ATOS). SGO uses the same model set-up as for SGS, but with different weights (see Bao et al. (2020) and Feser and Evangelou (2024)). The penalties are given by (for a group  $g$  and variable  $i$ , with  $p$  variables and  $m$  groups):

$$v_i = \sigma_1 + \sigma_2(p - i), \quad w_g = \sigma_1 + \sigma_3(m - g),$$

where

$$\sigma_1 = d_i \|X^T y\|_\infty, \quad \sigma_2 = \sigma_1/p, \quad \sigma_3 = \sigma_1/m, \quad d_i = i \times \exp(-2).$$

## Value

A list containing:

|                    |   |
|--------------------|---|
| beta               | The fitted values from the regression. Taken to be the more stable fit between $x$ and $z$ , which is usually the former. A filter is applied to remove very small values, where ATOS has not been able to shrink exactly to zero. Check this against $x$ and $z$ . |
| group_effects      | The group values from the regression. Taken by applying the $\ell_2$ norm within each group on beta.  |
| selected_var       | A list containing the indices of the active/selected variables for each "lambda" value. Index 1 corresponds to the first column in $X$ .  |
| selected_grp       | A list containing the indices of the active/selected groups for each "lambda" value. Index 1 corresponds to the first group in the groups vector.   |
| num_it             | Number of iterations performed. If convergence is not reached, this will be <code>max_iter</code> .   |
| success            | Logical flag indicating whether ATOS converged, according to <code>tol</code> .   |
| certificate        | Final value of convergence criteria.  |
| x                  | The solution to the original problem (see Pedregosa and Gidel (2018)).  |
| z                  | The updated values from applying the first proximal operator (see Pedregosa and Gidel (2018)).  |
| u                  | The solution to the dual problem (see Pedregosa and Gidel (2018)).  |
| screen_set_var     | List of variables that were kept after screening step for each "lambda" value. (corresponds to $\mathcal{S}_v$ in Feser and Evangelou (2024)).  |
| screen_set_grp     | List of groups that were kept after screening step for each "lambda" value. (corresponds to $\mathcal{S}_g$ in Feser and Evangelou (2024)).   |
| epsilon_set_var    | List of variables that were used for fitting after screening for each "lambda" value. (corresponds to $\mathcal{E}_v$ in Feser and Evangelou (2024)).   |
| epsilon_set_grp    | List of groups that were used for fitting after screening for each "lambda" value. (corresponds to $\mathcal{E}_g$ in Feser and Evangelou (2024)).  |
| kkt_violations_var | List of variables that violated the KKT conditions each "lambda" value. (corresponds to $\mathcal{K}_v$ in Feser and Evangelou (2024)).   |

|                    |  |
|--------------------|--|
| kkt_violations_grp | List of groups that violated the KKT conditions each "lambda" value. (corresponds to $\mathcal{K}_g$ in Feser and Evangelou (2024)). |
| pen_slope          | Vector of the variable penalty sequence.   |
| pen_gslope         | Vector of the group penalty sequence.  |
| screen             | Logical flag indicating whether screening was performed.   |
| type               | Indicates which type of regression was performed.  |
| intercept          | Logical flag indicating whether an intercept was fit.  |
| lambda             | Value(s) of $\lambda$ used to fit the model.   |

## References

- Bao, R., Gu B., Huang, H. (2020). *Fast OSCAR and OWL Regression via Safe Screening Rules*, <https://proceedings.mlr.press/v119/bao20b>
- Feser, F., Evangelou, M. (2023). *Sparse-group SLOPE: adaptive bi-level selection with FDR-control*, <https://arxiv.org/abs/2305.09467>
- Feser, F., Evangelou, M. (2024). *Strong screening rules for group-based SLOPE models*, <https://arxiv.org/abs/2405.15357>
- Pedregosa, F., Gidel, G. (2018). *Adaptive Three Operator Splitting*, <https://proceedings.mlr.press/v80/pedregosa18a.html>

## See Also

Other SGS-methods: [as\\_sgs\(\)](#), [coef.sgs\(\)](#), [fit\\_sgo\\_cv\(\)](#), [fit\\_sgs\(\)](#), [fit\\_sgs\\_cv\(\)](#), [plot.sgs\(\)](#), [predict.sgs\(\)](#), [print.sgs\(\)](#), [scaled\\_sgs\(\)](#)

## Examples

```
# specify a grouping structure
groups = c(1,1,1,2,2,3,3,3,4,4)
# generate data
data = gen_toy_data(p=10, n=5, groups = groups, seed_id=3,group_sparsity=1)
# run SGO
model = fit_sgo(X = data$X, y = data$y, groups = groups, type="linear", path_length = 5,
alpha=0.95, standardise = "l2", intercept = TRUE, verbose=FALSE)
```

---

fit\_sgo\_cv

*Fit an SGO model using k-fold cross-validation.*

---

## Description

Function to fit a pathwise solution of sparse-group SLOPE (SGO) models using k-fold cross-validation. Supports both linear and logistic regression, both with dense and sparse matrix implementations.

**Usage**

```

fit_sgo_cv(
  X,
  y,
  groups,
  type = "linear",
  lambda = "path",
  path_length = 20,
  min_frac = 0.05,
  alpha = 0.95,
  nfolds = 10,
  backtracking = 0.7,
  max_iter = 5000,
  max_iter_backtracking = 100,
  tol = 1e-05,
  standardise = "l2",
  intercept = TRUE,
  error_criteria = "mse",
  screen = TRUE,
  verbose = FALSE,
  v_weights = NULL,
  w_weights = NULL
)

```

**Arguments**

|             |   |
|-------------|---|
| X           | Input matrix of dimensions $n \times p$ . Can be a sparse matrix (using class "sparseMatrix" from the Matrix package).  |
| y           | Output vector of dimension $n$ . For type="linear" should be continuous and for type="logistic" should be a binary variable.  |
| groups      | A grouping structure for the input data. Should take the form of a vector of group indices.   |
| type        | The type of regression to perform. Supported values are: "linear" and "logistic".   |
| lambda      | The regularisation parameter. Defines the level of sparsity in the model. A higher value leads to sparser models: <ul style="list-style-type: none"> <li>"path" computes a path of regularisation parameters of length "path_length". The path will begin just above the value at which the first predictor enters the model and will terminate at the value determined by "min_frac".</li> <li>User-specified single value or sequence. Internal scaling is applied based on the type of standardisation. The returned "lambda" value will be the original unscaled value(s).</li> </ul> |
| path_length | The number of $\lambda$ values to fit the model for. If "lambda" is user-specified, this is ignored.  |
| min_frac    | Smallest value of $\lambda$ as a fraction of the maximum value. That is, the final $\lambda$ will be "min_frac" of the first $\lambda$ value.   |



|                       |   |
|-----------------------|---|
| alpha                 | The value of $\alpha$ , which defines the convex balance between OSCAR and gOSCAR. Must be between 0 and 1. Recommended value is 0.95.  |
| nfolds                | The number of folds to use in cross-validation.   |
| backtracking          | The backtracking parameter, $\tau$ , as defined in Pedregosa and Gidel (2018).  |
| max_iter              | Maximum number of ATOS iterations to perform.   |
| max_iter_backtracking | Maximum number of backtracking line search iterations to perform per global iteration.  |
| tol                   | Convergence tolerance for the stopping criteria.  |
| standardise           | Type of standardisation to perform on $X$ : <ul style="list-style-type: none"> <li>• "l2" standardises the input data to have <math>\ell_2</math> norms of one.</li> <li>• "l1" standardises the input data to have <math>\ell_1</math> norms of one.</li> <li>• "sd" standardises the input data to have standard deviation of one.</li> <li>• "none" no standardisation applied.</li> </ul> |
| intercept             | Logical flag for whether to fit an intercept.   |
| error_criteria        | The criteria used to discriminate between models along the path. Supported values are: "mse" (mean squared error) and "mae" (mean absolute error).  |
| screen                | Logical flag for whether to apply screening rules (see Feser and Evangelou (2024)). Screening discards irrelevant groups before fitting, greatly improving speed.   |
| verbose               | Logical flag for whether to print fitting information.  |
| v_weights             | Optional vector for the variable penalty weights. Overrides the OSCAR penalties when specified. When entering custom weights, these are multiplied internally by $\lambda$ and $\alpha$ . To void this behaviour, set $\lambda = 2$ and $\alpha = 0.5$ .  |
| w_weights             | Optional vector for the group penalty weights. Overrides the OSCAR penalties when specified. When entering custom weights, these are multiplied internally by $\lambda$ and $1 - \alpha$ . To void this behaviour, set $\lambda = 2$ and $\alpha = 0.5$ .   |

### Details

Fits SGO models under a pathwise solution using adaptive three operator splitting (ATOS), picking the lse model as optimum. Warm starts are implemented.

### Value

A list containing:

|                |  |
|----------------|--|
| all_models     | A list of all the models fitted along the path.                      |
| fit            | The lse chosen model, which is a "sgs" object type.                  |
| best_lambda    | The value of $\lambda$ which generated the chosen model.             |
| best_lambda_id | The path index for the chosen model.                                 |
| errors         | A table containing fitting information about the models on the path. |
| type           | Indicates which type of regression was performed.                    |

## References

- Bao, R., Gu B., Huang, H. (2020). *Fast OSCAR and OWL Regression via Safe Screening Rules*, <https://proceedings.mlr.press/v119/bao20b>
- Feser, F., Evangelou, M. (2023). *Sparse-group SLOPE: adaptive bi-level selection with FDR-control*, <https://arxiv.org/abs/2305.09467>
- Feser, F., Evangelou, M. (2024). *Strong screening rules for group-based SLOPE models*, <https://arxiv.org/abs/2405.15357>

## See Also

[fit\\_sgo\(\)](#)

Other model-selection: [as\\_sgs\(\)](#), [fit\\_goscar\\_cv\(\)](#), [fit\\_gslope\\_cv\(\)](#), [fit\\_sgs\\_cv\(\)](#), [scaled\\_sgs\(\)](#)

Other SGS-methods: [as\\_sgs\(\)](#), [coef.sgs\(\)](#), [fit\\_sgo\(\)](#), [fit\\_sgs\(\)](#), [fit\\_sgs\\_cv\(\)](#), [plot.sgs\(\)](#), [predict.sgs\(\)](#), [print.sgs\(\)](#), [scaled\\_sgs\(\)](#)

## Examples

```
# specify a grouping structure
groups = c(1,1,1,2,2,3,3,3,4,4)
# generate data
data = gen_toy_data(p=10, n=5, groups = groups, seed_id=3,group_sparsity=1)
# run SGO with cross-validation
cv_model = fit_sgo_cv(X = data$X, y = data$y, groups=groups, type = "linear",
path_length = 5, nfolds=5, alpha = 0.95, min_frac = 0.05,
standardise="l2", intercept=TRUE, verbose=TRUE)
```

---

fit\_sgs

*Fit an SGS model.*

---

## Description

Sparse-group SLOPE (SGS) main fitting function. Supports both linear and logistic regression, both with dense and sparse matrix implementations.

## Usage

```
fit_sgs(
  X,
  y,
  groups,
  type = "linear",
  lambda = "path",
  path_length = 20,
  min_frac = 0.05,
  alpha = 0.95,
  vFDR = 0.1,
```

```

gFDR = 0.1,
pen_method = 1,
max_iter = 5000,
backtracking = 0.7,
max_iter_backtracking = 100,
tol = 1e-05,
standardise = "l2",
intercept = TRUE,
screen = TRUE,
verbose = FALSE,
w_weights = NULL,
v_weights = NULL
)

```

### Arguments

|             |   |
|-------------|---|
| X           | Input matrix of dimensions $n \times p$ . Can be a sparse matrix (using class "sparseMatrix" from the Matrix package).  |
| y           | Output vector of dimension $n$ . For type="linear" should be continuous and for type="logistic" should be a binary variable.  |
| groups      | A grouping structure for the input data. Should take the form of a vector of group indices.   |
| type        | The type of regression to perform. Supported values are: "linear" and "logistic".   |
| lambda      | The regularisation parameter. Defines the level of sparsity in the model. A higher value leads to sparser models: <ul style="list-style-type: none"> <li>"path" computes a path of regularisation parameters of length "path_length". The path will begin just above the value at which the first predictor enters the model and will terminate at the value determined by "min_frac".</li> <li>User-specified single value or sequence. Internal scaling is applied based on the type of standardisation. The returned "lambda" value will be the original unscaled value(s).</li> </ul> |
| path_length | The number of $\lambda$ values to fit the model for. If "lambda" is user-specified, this is ignored.  |
| min_frac    | Smallest value of $\lambda$ as a fraction of the maximum value. That is, the final $\lambda$ will be "min_frac" of the first $\lambda$ value.   |
| alpha       | The value of $\alpha$ , which defines the convex balance between SLOPE and gSLOPE. Must be between 0 and 1. Recommended value is 0.95.  |
| vFDR        | Defines the desired variable false discovery rate (FDR) level, which determines the shape of the variable penalties. Must be between 0 and 1.   |
| gFDR        | Defines the desired group false discovery rate (FDR) level, which determines the shape of the group penalties. Must be between 0 and 1.   |
| pen_method  | The type of penalty sequences to use (see Feser and Evangelou (2023)): <ul style="list-style-type: none"> <li>"1" uses the vMean SGS and gMean gSLOPE sequences.</li> <li>"2" uses the vMax SGS and gMean gSLOPE sequences.</li> </ul>  |

|                       |  |
|-----------------------|--|
|                       | <ul style="list-style-type: none"> <li>• "3" uses the BH SLOPE and gMean gSLOPE sequences, also known as SGS Original.</li> </ul>  |
| max_iter              | Maximum number of ATOS iterations to perform.  |
| backtracking          | The backtracking parameter, $\tau$ , as defined in Pedregosa and Gidel (2018).   |
| max_iter_backtracking | Maximum number of backtracking line search iterations to perform per global iteration.   |
| tol                   | Convergence tolerance for the stopping criteria.   |
| standardise           | Type of standardisation to perform on $X$ : <ul style="list-style-type: none"> <li>• "l2" standardises the input data to have <math>\ell_2</math> norms of one. When using this "lambda" is scaled internally by <math>1/\sqrt{n}</math>.</li> <li>• "l1" standardises the input data to have <math>\ell_1</math> norms of one. When using this "lambda" is scaled internally by <math>1/n</math>.</li> <li>• "sd" standardises the input data to have standard deviation of one.</li> <li>• "none" no standardisation applied.</li> </ul> |
| intercept             | Logical flag for whether to fit an intercept.  |
| screen                | Logical flag for whether to apply screening rules (see Feser and Evangelou (2024)). Screening discards irrelevant groups before fitting, greatly improving speed.  |
| verbose               | Logical flag for whether to print fitting information.   |
| w_weights             | Optional vector for the group penalty weights. Overrides the penalties from pen_method if specified. When entering custom weights, these are multiplied internally by $\lambda$ and $1 - \alpha$ . To void this behaviour, set $\lambda = 2$ and $\alpha = 0.5$ .  |
| v_weights             | Optional vector for the variable penalty weights. Overrides the penalties from pen_method if specified. When entering custom weights, these are multiplied internally by $\lambda$ and $\alpha$ . To void this behaviour, set $\lambda = 2$ and $\alpha = 0.5$ .   |

## Details

`fit_sgs()` fits an SGS model (Feser and Evangelou (2023)) using adaptive three operator splitting (ATOS). SGS is a sparse-group method, so that it selects both variables and groups. Unlike group selection approaches, not every variable within a group is set as active. It solves the convex optimisation problem given by

$$\frac{1}{2n} f(b; y, \mathbf{X}) + \lambda \alpha \sum_{i=1}^p v_i |b|_{(i)} + \lambda (1 - \alpha) \sum_{g=1}^m w_g \sqrt{p_g} \|b^{(g)}\|_2,$$

where  $f(\cdot)$  is the loss function and  $p_g$  are the group sizes. The penalty parameters in SGS are sorted so that the largest coefficients are matched with the largest penalties, to reduce the FDR. For the variables:  $|\beta|_{(1)} \geq \dots \geq |\beta|_{(p)}$  and  $v_1 \geq \dots \geq v_p \geq 0$ . For the groups:  $\sqrt{p_1} \|\beta^{(1)}\|_2 \geq \dots \geq \sqrt{p_m} \|\beta^{(m)}\|_2$  and  $w_1 \geq \dots \geq w_m \geq 0$ . In the case of the linear model, the loss function is given by the mean-squared error loss:

$$f(b; y, \mathbf{X}) = \|y - \mathbf{X}b\|_2^2.$$

In the logistic model, the loss function is given by

$$f(b; y, \mathbf{X}) = -1/n \log(\mathcal{L}(b; y, \mathbf{X})).$$

where the log-likelihood is given by

$$\mathcal{L}(b; y, \mathbf{X}) = \sum_{i=1}^n \{y_i b^\top x_i - \log(1 + \exp(b^\top x_i))\}.$$

SGS can be seen to be a convex combination of SLOPE and gSLOPE, balanced through alpha, such that it reduces to SLOPE for alpha = 0 and to gSLOPE for alpha = 1. The penalty parameters in SGS are sorted so that the largest coefficients are matched with the largest penalties, to reduce the FDR. For the group penalties, see `fit_gslope()`. For the variable penalties, the vMean SGS sequence (pen\_method=1) (Feser and Evangelou (2023)) is given by

$$v_i^{\text{mean}} = \bar{F}_{\mathcal{N}}^{-1} \left( 1 - \frac{q_v i}{2p} \right), \text{ where } \bar{F}_{\mathcal{N}}(x) := \frac{1}{m} \sum_{j=1}^m F_{\mathcal{N}} \left( \alpha x + \frac{1}{3}(1 - \alpha)a_j w_j \right), \quad i = 1, \dots, p,$$

where  $F_{\mathcal{N}}$  is the cumulative distribution functions of a standard Gaussian distribution. The vMax SGS sequence (pen\_method=2) (Feser and Evangelou (2023)) is given by

$$v_i^{\text{max}} = \max_{j=1, \dots, m} \left\{ \frac{1}{\alpha} F_{\mathcal{N}}^{-1} \left( 1 - \frac{q_v i}{2p} \right) - \frac{1}{3\alpha}(1 - \alpha)a_j w_j \right\},$$

The BH SLOPE sequence (pen\_method=3) (Bogdan et al. (2015)) is given by

$$v_i = z(1 - iq_v/2p),$$

where  $z$  is the quantile function of a standard normal distribution.

## Value

A list containing:

|               |   |
|---------------|---|
| beta          | The fitted values from the regression. Taken to be the more stable fit between x and z, which is usually the former. A filter is applied to remove very small values, where ATOS has not been able to shrink exactly to zero. Check this against x and z. |
| group_effects | The group values from the regression. Taken by applying the $\ell_2$ norm within each group on beta.  |
| selected_var  | A list containing the indices of the active/selected variables for each "lambda" value. Index 1 corresponds to the first column in X.   |
| selected_grp  | A list containing the indices of the active/selected groups for each "lambda" value. Index 1 corresponds to the first group in the groups vector.   |
| num_it        | Number of iterations performed. If convergence is not reached, this will be max_iter.   |
| success       | Logical flag indicating whether ATOS converged, according to tol.   |
| certificate   | Final value of convergence criteria.  |

|                    |   |
|--------------------|---|
| x                  | The solution to the original problem (see Pedregosa and Gidel (2018)).  |
| z                  | The updated values from applying the first proximal operator (see Pedregosa and Gidel (2018)).  |
| u                  | The solution to the dual problem (see Pedregosa and Gidel (2018)).  |
| screen_set_var     | List of variables that were kept after screening step for each "lambda" value. (corresponds to $\mathcal{S}_v$ in Feser and Evangelou (2024)).        |
| screen_set_grp     | List of groups that were kept after screening step for each "lambda" value. (corresponds to $\mathcal{S}_g$ in Feser and Evangelou (2024)).           |
| epsilon_set_var    | List of variables that were used for fitting after screening for each "lambda" value. (corresponds to $\mathcal{E}_v$ in Feser and Evangelou (2024)). |
| epsilon_set_grp    | List of groups that were used for fitting after screening for each "lambda" value. (corresponds to $\mathcal{E}_g$ in Feser and Evangelou (2024)).    |
| kkt_violations_var | List of variables that violated the KKT conditions each "lambda" value. (corresponds to $\mathcal{K}_v$ in Feser and Evangelou (2024)).               |
| kkt_violations_grp | List of groups that violated the KKT conditions each "lambda" value. (corresponds to $\mathcal{K}_g$ in Feser and Evangelou (2024)).                  |
| pen_slope          | Vector of the variable penalty sequence.  |
| pen_gslope         | Vector of the group penalty sequence.   |
| screen             | Logical flag indicating whether screening was performed.  |
| type               | Indicates which type of regression was performed.   |
| intercept          | Logical flag indicating whether an intercept was fit.   |
| lambda             | Value(s) of $\lambda$ used to fit the model.  |

## References

- Bogdan, M., van den Berg, E., Sabatti, C., Candes, E. (2015). *SLOPE - Adaptive variable selection via convex optimization*, <https://projecteuclid.org/journals/annals-of-applied-statistics/volume-9/issue-3/SLOPEAdaptive-variable-selection-via-convex-optimization/10.1214/15-A0AS842.full>
- Feser, F., Evangelou, M. (2023). *Sparse-group SLOPE: adaptive bi-level selection with FDR-control*, <https://arxiv.org/abs/2305.09467>
- Feser, F., Evangelou, M. (2024). *Strong screening rules for group-based SLOPE models*, <https://arxiv.org/abs/2405.15357>
- Pedregosa, F., Gidel, G. (2018). *Adaptive Three Operator Splitting*, <https://proceedings.mlr.press/v80/pedregosa18a.html>

## See Also

Other SGS-methods: `as_sgs()`, `coef.sgs()`, `fit_sgo()`, `fit_sgo_cv()`, `fit_sgs_cv()`, `plot.sgs()`, `predict.sgs()`, `print.sgs()`, `scaled_sgs()`

## Examples

```
# specify a grouping structure
groups = c(1,1,1,2,2,3,3,3,4,4)
# generate data
data = gen_toy_data(p=10, n=5, groups = groups, seed_id=3,group_sparsity=1)
# run SGS
model = fit_sgs(X = data$X, y = data$y, groups = groups, type="linear", path_length = 5,
alpha=0.95, vFDR=0.1, gFDR=0.1, standardise = "l2", intercept = TRUE, verbose=FALSE)
```

---

fit\_sgs\_cv

*Fit an SGS model using k-fold cross-validation.*

---

## Description

Function to fit a pathwise solution of sparse-group SLOPE (SGS) models using k-fold cross-validation. Supports both linear and logistic regression, both with dense and sparse matrix implementations.

## Usage

```
fit_sgs_cv(
  X,
  y,
  groups,
  type = "linear",
  lambda = "path",
  path_length = 20,
  min_frac = 0.05,
  alpha = 0.95,
  vFDR = 0.1,
  gFDR = 0.1,
  pen_method = 1,
  nfolds = 10,
  backtracking = 0.7,
  max_iter = 5000,
  max_iter_backtracking = 100,
  tol = 1e-05,
  standardise = "l2",
  intercept = TRUE,
  error_criteria = "mse",
  screen = TRUE,
  verbose = FALSE,
  v_weights = NULL,
  w_weights = NULL
)
```

**Arguments**

|                       |   |
|-----------------------|---|
| X                     | Input matrix of dimensions $n \times p$ . Can be a sparse matrix (using class "sparseMatrix" from the Matrix package).  |
| y                     | Output vector of dimension $n$ . For type="linear" should be continuous and for type="logistic" should be a binary variable.  |
| groups                | A grouping structure for the input data. Should take the form of a vector of group indices.   |
| type                  | The type of regression to perform. Supported values are: "linear" and "logistic".   |
| lambda                | The regularisation parameter. Defines the level of sparsity in the model. A higher value leads to sparser models: <ul style="list-style-type: none"> <li>• "path" computes a path of regularisation parameters of length "path_length". The path will begin just above the value at which the first predictor enters the model and will terminate at the value determined by "min_frac".</li> <li>• User-specified single value or sequence. Internal scaling is applied based on the type of standardisation. The returned "lambda" value will be the original unscaled value(s).</li> </ul> |
| path_length           | The number of $\lambda$ values to fit the model for. If "lambda" is user-specified, this is ignored.  |
| min_frac              | Smallest value of $\lambda$ as a fraction of the maximum value. That is, the final $\lambda$ will be "min_frac" of the first $\lambda$ value.   |
| alpha                 | The value of $\alpha$ , which defines the convex balance between SLOPE and gSLOPE. Must be between 0 and 1. Recommended value is 0.95.  |
| vFDR                  | Defines the desired variable false discovery rate (FDR) level, which determines the shape of the variable penalties. Must be between 0 and 1.   |
| gFDR                  | Defines the desired group false discovery rate (FDR) level, which determines the shape of the group penalties. Must be between 0 and 1.   |
| pen_method            | The type of penalty sequences to use (see Feser and Evangelou (2023)): <ul style="list-style-type: none"> <li>• "1" uses the vMean SGS and gMean gSLOPE sequences.</li> <li>• "2" uses the vMax SGS and gMean gSLOPE sequences.</li> <li>• "3" uses the BH SLOPE and gMean gSLOPE sequences, also known as SGS Original.</li> </ul>   |
| nfolds                | The number of folds to use in cross-validation.   |
| backtracking          | The backtracking parameter, $\tau$ , as defined in Pedregosa and Gidel (2018).  |
| max_iter              | Maximum number of ATOS iterations to perform.   |
| max_iter_backtracking | Maximum number of backtracking line search iterations to perform per global iteration.  |
| tol                   | Convergence tolerance for the stopping criteria.  |
| standardise           | Type of standardisation to perform on X: <ul style="list-style-type: none"> <li>• "l2" standardises the input data to have <math>\ell_2</math> norms of one.</li> <li>• "l1" standardises the input data to have <math>\ell_1</math> norms of one.</li> </ul>   |



- "sd" standardises the input data to have standard deviation of one.
- "none" no standardisation applied.

|                |   |
|----------------|---|
| intercept      | Logical flag for whether to fit an intercept.   |
| error_criteria | The criteria used to discriminate between models along the path. Supported values are: "mse" (mean squared error) and "mae" (mean absolute error).  |
| screen         | Logical flag for whether to apply screening rules (see Feser and Evangelou (2024)). Screening discards irrelevant groups before fitting, greatly improving speed.   |
| verbose        | Logical flag for whether to print fitting information.  |
| v_weights      | Optional vector for the variable penalty weights. Overrides the penalties from pen_method if specified. When entering custom weights, these are multiplied internally by $\lambda$ and $\alpha$ . To void this behaviour, set $\lambda = 2$ and $\alpha = 0.5$  |
| w_weights      | Optional vector for the group penalty weights. Overrides the penalties from pen_method if specified. When entering custom weights, these are multiplied internally by $\lambda$ and $1 - \alpha$ . To void this behaviour, set $\lambda = 2$ and $\alpha = 0.5$ |

### Details

Fits SGS models under a pathwise solution using adaptive three operator splitting (ATOS), picking the lse model as optimum. Warm starts are implemented.

### Value

A list containing:

|                |  |
|----------------|--|
| all_models     | A list of all the models fitted along the path.                      |
| fit            | The lse chosen model, which is a "sgs" object type.                  |
| best_lambda    | The value of $\lambda$ which generated the chosen model.             |
| best_lambda_id | The path index for the chosen model.                                 |
| errors         | A table containing fitting information about the models on the path. |
| type           | Indicates which type of regression was performed.                    |

### References

Feser, F., Evangelou, M. (2023). *Sparse-group SLOPE: adaptive bi-level selection with FDR-control*, <https://arxiv.org/abs/2305.09467>

Feser, F., Evangelou, M. (2024). *Strong screening rules for group-based SLOPE models*, <https://arxiv.org/abs/2405.15357>

### See Also

[fit\\_sgs\(\)](#)

Other model-selection: [as\\_sgs\(\)](#), [fit\\_goscar\\_cv\(\)](#), [fit\\_gslope\\_cv\(\)](#), [fit\\_sgo\\_cv\(\)](#), [scaled\\_sgs\(\)](#)

Other SGS-methods: [as\\_sgs\(\)](#), [coef.sgs\(\)](#), [fit\\_sgo\(\)](#), [fit\\_sgo\\_cv\(\)](#), [fit\\_sgs\(\)](#), [plot.sgs\(\)](#), [predict.sgs\(\)](#), [print.sgs\(\)](#), [scaled\\_sgs\(\)](#)

## Examples

```
# specify a grouping structure
groups = c(1,1,1,2,2,3,3,3,4,4)
# generate data
data = gen_toy_data(p=10, n=5, groups = groups, seed_id=3,group_sparsity=1)
# run SGS with cross-validation
cv_model = fit_sgs_cv(X = data$X, y = data$y, groups=groups, type = "linear",
path_length = 5, nfolds=5, alpha = 0.95, vFDR = 0.1, gFDR = 0.1, min_frac = 0.05,
standardise="l2",intercept=TRUE,verbose=TRUE)
```

---

|          |  |
|----------|--|
| gen_pens | <i>Generate penalty sequences for SGS.</i> |
|----------|--|

---

## Description

Generates variable and group penalties for SGS.

## Usage

```
gen_pens(gFDR, vFDR, pen_method, groups, alpha)
```

## Arguments

|            |  |
|------------|--|
| gFDR       | Defines the desired group false discovery rate (FDR) level, which determines the shape of the group penalties.   |
| vFDR       | Defines the desired variable false discovery rate (FDR) level, which determines the shape of the variable penalties.   |
| pen_method | The type of penalty sequences to use (see Feser and Evangelou (2023)): <ul style="list-style-type: none"> <li>• "1" uses the vMean SGS and gMean gSLOPE sequences.</li> <li>• "2" uses the vMax SGS and gMean gSLOPE sequences.</li> <li>• "3" uses the BH SLOPE and gMean gSLOPE sequences, also known as SGS Original.</li> <li>• "4" uses the gMax gSLOPE sequence. For a gSLOPE model only.</li> </ul> |
| groups     | A grouping structure for the input data. Should take the form of a vector of group indices.  |
| alpha      | The value of $\alpha$ , defines the convex balance between SLOPE and gSLOPE.   |

## Details

The vMean and vMax SGS sequences are variable sequences derived specifically to give variable false discovery rate (FDR) control for SGS under orthogonal designs (see Feser and Evangelou (2023)). The BH SLOPE sequence is derived in Bodgan et al. (2015) and has links to the Benjamini-Hochberg critical values. The sequence provides variable FDR-control for SLOPE under orthogonal designs. The gMean gSLOPE sequence is derived in Brzyski et al. (2015) and provides group FDR-control for gSLOPE under orthogonal designs.

**Value**

A list containing:

pen\_slope\_org A vector of the variable penalty sequence.

pen\_gslope\_org A vector of the group penalty sequence.

**References**

Bogdan, M., Van den Berg, E., Sabatti, C., Su, W., Candes, E. (2015). *SLOPE — Adaptive variable selection via convex optimization*, <https://projecteuclid.org/journals/annals-of-applied-statistics/volume-9/issue-3/SLOPEAdaptive-variable-selection-via-convex-optimization/10.1214/15-A0AS842.full>

Brzyski, D., Gossmann, A., Su, W., Bodgan, M. (2019). *Group SLOPE – Adaptive Selection of Groups of Predictors*, <https://www.tandfonline.com/doi/full/10.1080/01621459.2017.1411269>

Feser, F., Evangelou, M. (2023). *Sparse-group SLOPE: adaptive bi-level selection with FDR-control*, <https://arxiv.org/abs/2305.09467>

**Examples**

```
# specify a grouping structure
groups = c(rep(1:20, each=3),
           rep(21:40, each=4),
           rep(41:60, each=5),
           rep(61:80, each=6),
           rep(81:100, each=7))
# generate sequences
sequences = gen_pens(gFDR=0.1, vFDR=0.1, pen_method=1, groups=groups, alpha=0.5)
```

---

|              |                           |
|--------------|---------------------------|
| gen_toy_data | <i>Generate toy data.</i> |
|--------------|---------------------------|

---

**Description**

Generates different types of datasets, which can then be fitted using sparse-group SLOPE.

**Usage**

```
gen_toy_data(
  p,
  n,
  rho = 0,
  seed_id = 2,
  grouped = TRUE,
  groups,
  noise_level = 1,
```

```

group_sparsity = 0.1,
var_sparsity = 0.5,
orthogonal = FALSE,
data_mean = 0,
data_sd = 1,
signal_mean = 0,
signal_sd = sqrt(10)
)

```

### Arguments

|                |   |
|----------------|---|
| p              | The number of input variables.  |
| n              | The number of observations.   |
| rho            | Correlation coefficient. Must be in range [0, 1].   |
| seed_id        | Seed to be used to generate the data matrix $X$ .   |
| grouped        | A logical flag indicating whether grouped data is required.   |
| groups         | If grouped=TRUE, the grouping structure is required. Each input variable should have a group id.  |
| noise_level    | Defines the level of noise ( $\sigma$ ) to be used in generating the response vector $y$ .  |
| group_sparsity | Defines the level of group sparsity. Must be in the range [0, 1].   |
| var_sparsity   | Defines the level of variable sparsity. Must be in the range [0, 1]. If grouped=TRUE, this defines the level of sparsity within each group, not globally. |
| orthogonal     | Logical flag as to whether the input matrix should be orthogonal.   |
| data_mean      | Defines the mean of input predictors.   |
| data_sd        | Defines the standard deviation of the signal ( $\beta$ ).   |
| signal_mean    | Defines the mean of the signal ( $\beta$ ).   |
| signal_sd      | Defines the standard deviation of the signal ( $\beta$ ).   |

### Details

The data is generated under a Gaussian linear model. The generated data can be grouped and sparsity can be provided at both a group and/or variable level.

### Value

A list containing:

|             |   |
|-------------|---|
| y           | The response vector.                                      |
| X           | The input matrix.   |
| true_beta   | The true values of $\beta$ used to generate the response. |
| true_grp_id | Indices of which groups are non-zero in true_beta.        |

**Examples**

```
# specify a grouping structure
groups = c(rep(1:20, each=3),
           rep(21:40, each=4),
           rep(41:60, each=5),
           rep(61:80, each=6),
           rep(81:100, each=7))
# generate data
data = gen_toy_data(p=500, n=400, groups = groups, seed_id=3)
```

---

|          |   |
|----------|---|
| plot.sgs | <i>Plot models of the following object types: "sgs", "sgs_cv", "gslope", "gslope_cv".</i> |
|----------|---|

---

**Description**

Plots the pathwise solution of a cross-validation fit, from a call to one of the following: `fit_sgs()`, `fit_sgs_cv()`, `fit_gslope()`, `fit_gslope_cv()`, `fit_sgo()`, `fit_sgo_cv()`, `fit_goscar()`, `fit_goscar_cv()`.

**Usage**

```
## S3 method for class 'sgs'
plot(x, how_many = 10, ...)
```

**Arguments**

|          |  |
|----------|--|
| x        | Object of one of the following classes: "sgs", "sgs_cv", "gslope", "gslope_cv".                          |
| how_many | Defines how many predictors to plot. Plots the predictors in decreasing order of largest absolute value. |
| ...      | further arguments passed to base function.   |

**Value**

A list containing:

|          |  |
|----------|--|
| response | The predicted response. In the logistic case, this represents the predicted class probabilities. |
| class    | The predicted class assignments. Only returned if type = "logistic" in the model object.         |

**See Also**

`fit_sgs()`, `fit_sgs_cv()`, `fit_gslope()`, `fit_gslope_cv()`, `fit_sgo()`, `fit_sgo_cv()`, `fit_goscar()`, `fit_goscar_cv()`

Other SGS-methods: `as_sgs()`, `coef.sgs()`, `fit_sgo()`, `fit_sgo_cv()`, `fit_sgs()`, `fit_sgs_cv()`, `predict.sgs()`, `print.sgs()`, `scaled_sgs()`

Other gSLOPE-methods: `coef.sgs()`, `fit_goscar()`, `fit_goscar_cv()`, `fit_gslope()`, `fit_gslope_cv()`, `predict.sgs()`, `print.sgs()`

**Examples**

```
# specify a grouping structure
groups = c(1,1,2,2,3)
# generate data
data = gen_toy_data(p=5, n=4, groups = groups, seed_id=3, signal_mean=20, group_sparsity=1)
# run SGS
model = fit_sgs(X = data$X, y = data$y, groups=groups, type = "linear",
path_length = 20, alpha = 0.95, vFDR = 0.1, gFDR = 0.1,
min_frac = 0.05, standardise="l2", intercept=TRUE, verbose=FALSE)
plot(model, how_many = 10)
```

---

|             |   |
|-------------|---|
| predict.sgs | <i>Predict using one of the following object types: "sgs", "sgs_cv", "gslope", "gslope_cv".</i> |
|-------------|---|

---

**Description**

Performs prediction from one of the following fits: `fit_sgs()`, `fit_sgs_cv()`, `fit_gslope()`, `fit_gslope_cv()`, `fit_sgo()`, `fit_sgo_cv()`, `fit_goscar()`, `fit_goscar_cv()`. The predictions are calculated for each "lambda" value in the path.

**Usage**

```
## S3 method for class 'sgs'
predict(object, x, ...)
```

**Arguments**

|        |   |
|--------|---|
| object | Object of one of the following classes: "sgs", "sgs_cv", "gslope", "gslope_cv". |
| x      | Input data to use for prediction.   |
| ...    | further arguments passed to stats function.                                     |

**Value**

A list containing:

|          |  |
|----------|--|
| response | The predicted response. In the logistic case, this represents the predicted class probabilities. |
| class    | The predicted class assignments. Only returned if type = "logistic" in the model object.         |

**See Also**

`fit_sgs()`, `fit_sgs_cv()`, `fit_gslope()`, `fit_gslope_cv()`, `fit_sgo()`, `fit_sgo_cv()`, `fit_goscar()`, `fit_goscar_cv()`

Other SGS-methods: `as_sgs()`, `coef.sgs()`, `fit_sgo()`, `fit_sgo_cv()`, `fit_sgs()`, `fit_sgs_cv()`, `plot.sgs()`, `print.sgs()`, `scaled_sgs()`

Other gSLOPE-methods: `coef.sgs()`, `fit_goscar()`, `fit_goscar_cv()`, `fit_gslope()`, `fit_gslope_cv()`, `plot.sgs()`, `print.sgs()`

**Examples**

```
# specify a grouping structure
groups = c(1,1,1,2,2,3,3,3,4,4)
# generate data
data = gen_toy_data(p=10, n=5, groups = groups, seed_id=3,group_sparsity=1)
# run SGS
model = fit_sgs(X = data$X, y = data$y, groups = groups, type="linear", lambda = 1, alpha=0.95,
vFDR=0.1, gFDR=0.1, standardise = "l2", intercept = TRUE, verbose=FALSE)
# use predict function
model_predictions = predict(model, x = data$X)
```

---

|           |  |
|-----------|--|
| print.sgs | <i>Prints information for one of the following object types: "sgs", "sgs_cv", "gslope", "gslope_cv".</i> |
|-----------|--|

---

**Description**

Prints out useful metric from a model fit.

**Usage**

```
## S3 method for class 'sgs'
print(x, ...)
```

**Arguments**

`x` Object of one of the following classes: "sgs", "sgs\_cv", "gslope", "gslope\_cv".  
`...` further arguments passed to base function.

**Value**

A summary of the model fit(s).

**See Also**

[fit\\_sgs\(\)](#), [fit\\_sgs\\_cv\(\)](#), [fit\\_gslope\(\)](#), [fit\\_gslope\\_cv\(\)](#), [fit\\_sgo\(\)](#), [fit\\_sgo\\_cv\(\)](#), [fit\\_goscar\(\)](#), [fit\\_goscar\\_cv\(\)](#)

Other SGS-methods: [as\\_sgs\(\)](#), [coef.sgs\(\)](#), [fit\\_sgo\(\)](#), [fit\\_sgo\\_cv\(\)](#), [fit\\_sgs\(\)](#), [fit\\_sgs\\_cv\(\)](#), [plot.sgs\(\)](#), [predict.sgs\(\)](#), [scaled\\_sgs\(\)](#)

Other gSLOPE-methods: [coef.sgs\(\)](#), [fit\\_goscar\(\)](#), [fit\\_goscar\\_cv\(\)](#), [fit\\_gslope\(\)](#), [fit\\_gslope\\_cv\(\)](#), [plot.sgs\(\)](#), [predict.sgs\(\)](#)

**Examples**

```
# specify a grouping structure
groups = c(rep(1:20, each=3),
           rep(21:40, each=4),
           rep(41:60, each=5),
           rep(61:80, each=6),
           rep(81:100, each=7))

# generate data
data = gen_toy_data(p=500, n=400, groups = groups, seed_id=3)
# run SGS
model = fit_sgs(X = data$X, y = data$y, groups = groups, type="linear", lambda = 1, alpha=0.95,
               vFDR=0.1, gFDR=0.1, standardise = "l2", intercept = TRUE, verbose=FALSE)
# print model
print(model)
```

---

scaled\_sgs

*Fits a scaled SGS model.*

---

**Description**

Fits an SGS model using the noise estimation procedure (Algorithm 5 from Bogdan et al. (2015)). This estimates  $\lambda$  and then fits the model using the estimated value. It is an alternative approach to cross-validation ([fit\\_sgs\\_cv\(\)](#)).

**Usage**

```
scaled_sgs(
  X,
  y,
  groups,
  type = "linear",
  pen_method = 1,
  alpha = 0.95,
  vFDR = 0.1,
  gFDR = 0.1,
  standardise = "l2",
  intercept = TRUE,
  verbose = FALSE
)
```



**Arguments**

|             |  |
|-------------|--|
| X           | Input matrix of dimensions $n \times p$ . Can be a sparse matrix (using class "sparseMatrix" from the Matrix package).   |
| y           | Output vector of dimension $n$ . For type="linear" should be continuous and for type="logistic" should be a binary variable.   |
| groups      | A grouping structure for the input data. Should take the form of a vector of group indices.  |
| type        | The type of regression to perform. Supported values are: "linear" and "logistic".  |
| pen_method  | The type of penalty sequences to use. <ul style="list-style-type: none"> <li>• "1" uses the vMean SGS and gMean gSLOPE sequences.</li> <li>• "2" uses the vMax SGS and gMean gSLOPE sequences.</li> <li>• "1" uses the BH SLOPE and gMean gSLOPE sequences, also known as SGS Original.</li> </ul>   |
| alpha       | The value of $\alpha$ , which defines the convex balance between SLOPE and gSLOPE. Must be between 0 and 1.  |
| vFDR        | Defines the desired variable false discovery rate (FDR) level, which determines the shape of the variable penalties. Must be between 0 and 1.  |
| gFDR        | Defines the desired group false discovery rate (FDR) level, which determines the shape of the group penalties. Must be between 0 and 1.  |
| standardise | Type of standardisation to perform on X: <ul style="list-style-type: none"> <li>• "l2" standardises the input data to have <math>\ell_2</math> norms of one.</li> <li>• "l1" standardises the input data to have <math>\ell_1</math> norms of one.</li> <li>• "sd" standardises the input data to have standard deviation of one.</li> <li>• "none" no standardisation applied.</li> </ul> |
| intercept   | Logical flag for whether to fit an intercept.  |
| verbose     | Logical flag for whether to print fitting information.   |

**Value**

An object of type "sgs" containing model fit information (see [fit\\_sgs\(\)](#)).

**References**

Bogdan, M., Van den Berg, E., Sabatti, C., Su, W., Candes, E. (2015). *SLOPE — Adaptive variable selection via convex optimization*, <https://projecteuclid.org/journals/annals-of-applied-statistics/volume-9/issue-3/SLOPEAdaptive-variable-selection-via-convex-optimization/10.1214/15-A0AS842.full>

**See Also**

[as\\_sgs\(\)](#)

Other model-selection: [as\\_sgs\(\)](#), [fit\\_goscar\\_cv\(\)](#), [fit\\_gslope\\_cv\(\)](#), [fit\\_sgo\\_cv\(\)](#), [fit\\_sgs\\_cv\(\)](#)

Other SGS-methods: [as\\_sgs\(\)](#), [coef.sgs\(\)](#), [fit\\_sgo\(\)](#), [fit\\_sgo\\_cv\(\)](#), [fit\\_sgs\(\)](#), [fit\\_sgs\\_cv\(\)](#), [plot.sgs\(\)](#), [predict.sgs\(\)](#), [print.sgs\(\)](#)

**Examples**

```
# specify a grouping structure
groups = c(1,1,2,2,3)
# generate data
data = gen_toy_data(p=5, n=4, groups = groups, seed_id=3,
signal_mean=20,group_sparsity=1,var_sparsity=1)
# run noise estimation
model = scaled_sgs(X=data$X, y=data$y, groups=groups, pen_method=1)
```

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